

COMP9517: Computer Vision

Feature Representation

Outline

- What and why of feature representation
- How of feature representation
	- Different feature extractors/descriptors
		- Classical approaches
		- Representation learning
	- Application cases in various computer vision applications

Why and What of Feature Representation

sea bass and salmon Classification?

sea bass and salmon

lightness

Feature representation for a cat detector? -- not always easy

Image Features

- Image features are essentially **vectors** that are a **compact representation** of images
- They represent important information shown in an image
- Intuitive examples of image features:
	- Colour/brightness
	- Edges
	- Corners
	- Lines
	- Shape
	- Texture
	- etc…

Image Features

- We need to represent images as feature vectors for further processing in a more efficient and robust way
	- Pixel values -> more informative representations
- Examples of further processing include:
	- Object detection
	- Image segmentation
	- Image classification
	- Content-based image retrieval
	- Image stitching
	- Object tracking

Image Classification

Object Detection

Segmentation

Content-Based Image Retrieval

Image Stitching

Object Tracking

[https://heartbeat.fritz.ai/](https://heartbeat.fritz.ai/the-5-computer-vision-techniques-that-will-change-how-you-see-the-world-1ee19334354b)

Properties of Features

- Why not just use pixels values directly?
	- Pixel values change with light intensity, colour and direction
	- They also change with camera orientation
	- And they are highly redundant
- Repeatability (robustness)
	- Should be detectable at the same locations in different images despite changes in illumination and viewpoint
- Saliency (descriptiveness)
	- Each feature should have a distinctive and matchable description
- Compactness (efficiency)
	- Fewer features
	- Smaller features

to tasks

May be irrelevant

General Framework

Object detection Image segmentation Image classification Image retrieval Image stitching Object tracking

…

How of Feature Representation

- Colour features (based on pixel value)
	- Colour histogram
	- Colour moments
- Feature Descriptors (based on pixel gradients/textures)
	- Haralick texture features
	- Local binary patterns (LBP)
	- Scale-invariant feature transform (SIFT)
	- Bag-of-words (BoW)
	- Histogram of oriented gradients (HOG)
	- Shape descriptors
- Learning based feature representation
	- Unsupervised representation learning
	- Supervised representation learning

Colour Features

- **Colour** is the simplest feature to compute, and is **invariant** to image scaling, translation and rotation
- Color-sensitive tasks
- Example: colour-based image retrieval

Colour Histogram

- Represent the global distribution of pixel colours in an image
	- Step 1: Construct a histogram for each colour channel (R, G, B)
	- Step 2: Concatenate the histograms (vectors) of all channels as the final feature vector

Colour Moments

fij is the value of the *i*-th colour component of pixel *j* and *N* is the number of pixels in the image

- Another way of representing colour distributions
	- Based on statistical moments (summarization of a whole image)

- Moments based representation of colour distributions
	- Gives a feature vector of only 9 elements (for RGB images)
	- Lower representation capability than the colour histogram

Application Example

• Colour-based image retrieval

Pixel Gradient-based Features

- Feature descriptor relying on local patterns at "textural" level.
- Local appearance reflected in pixel gradients
- **Texture** is a powerful discriminating feature for identifying **visual patterns** with properties of homogeneity that cannot result from the presence of only a single color or intensity
- Many successful classical feature descriptors

<https://arxiv.org/abs/1801.10324>

Haralick Features

- Haralick features give an **array of statistical descriptors** of image patterns to capture the **spatial relationship between neighbouring pixels**, that is, textures.
	- Step 1: Construct the **gray-level co-occurrence matrix** (GLCM)
	- Step 2: Compute the Haralick feature descriptors from the GLCM
- Representing the feel, appearance, or consistency of a surface, such as distinguishing rough and smooth surfaces.

- Describe the spatial structure of local image texture
	- Divide the image into cells of *N* x *N* pixels (e.g. *N* = 16 or 32)
	- Compare each pixel in a cell to each of its 8 neighbouring pixels: If the centre pixel's value is greater than the neighbour's value, write "0", otherwise write "1"
	- This gives an 8-digit binary pattern per pixel after comparing with all 8 neighbouring pixels, representing a value in the range 0…255

- Describe the spatial structure of local image texture (cont.)
	- Generate the histogram for all pixels in the cell, computing the frequency of each 8-digit binary number occurring in the cell
	- This gives a 256-bin histogram (the LBP feature vector)
	- Combine the histograms of all cells to obtain the image-level LBP feature descriptor

Ref: https://pyimagesearch.com/2015/12/07/local-binary-patterns-with-python-opencv/

- LBP can be multi-resolution and rotation-invariant
	- Multi-resolution: varying the distance between the centre pixel and neighbouring pixels, and the number of neighbouring pixels

T. Ojala, M. Pietikainen, and T. Maenpaa, "Multiresolution gray-scale and rotation invariant texture classification with local binary patterns," IEEE Transactions on Pattern Analysis and Machine Intelligence 24(7):971-987, 2002. <https://doi.org/10.1109/TPAMI.2002.1017623>

- LBP can be multi-resolution and rotation-invariant
	- Rotation-invariant: varying the way of constructing the 8-digit binary number, e.g. performing bitwise shift to derive the smallest number

Note: not all patterns have 8 shifted variants (e.g. 11001100 has only 4)

- LBP can be multi-resolution and rotation-invariant
	- Rotation-invariant: varying the way of constructing the 8-digit binary number, e.g. performing bitwise shift to derive the smallest number => this reduces the LBP feature dimension from 256 to 36

T. Ojala, M. Pietikainen, and T. Maenpaa, "Multiresolution gray-scale and rotation invariant texture classification with local binary patterns," IEEE Transactions on Pattern Analysis and Machine Intelligence 24(7):971-987, 2002. <https://doi.org/10.1109/TPAMI.2002.1017623>

Application Example

 LBP_{PR} $P_{i}R$ **RESULT BINS** 8.1 10 88.2 16.2 18 98.5 24,3 99.1 26 $8,1+16,2$ $10 + 18$ 99.0 $8,1+24,3$ $10+26$ 99.6 $16,2+24,3$ $18 + 26$ 99.0 $8,1+16,2+24,3$ $10+18+26$ 99.1

• Texture classification

Scale-Invariant Feature Transform

- SIFT feature describes the texture features in a localised region around a **key points** Distinctive image features from scale-invariant keypoints International journal of computer vision 60 (2), 91-110
- SIFT descriptor is invariant to uniform scaling, orientation, and partially invariant to affine distortion and illumination changes

70976

2004

SIFT Extrema Detection

- Difference of Gaussian (DoG) features at multiple scales
- Detect *maxima* and *minima* in the scale space of the image

D. G. Lowe, "Distinctive image features from scale-invariant keypoints," Int. J. Comput. Vis. 60(2):91-110, http://weitz.de/sift/ 31 November 2004.<https://doi.org/10.1023/B:VISI.0000029664.99615.94>

http://weitz.de/sift/

SIFT Keypoint Localization

- Improve and reduce the set of found keypoints
	- Use 3D quadratic fitting in scale-space to get **subpixel** optima
		- Taylor expansion of the scale-space function up to quadratic term
	- Reject low-contrast and edge points using Hessian analysis

Initial keypoints from scale-space optima

Keypoints after rejecting low-contrast points

Final keypoints after rejecting edge points

 $D(\mathbf{x}) = D + \frac{\partial D}{\partial \mathbf{x}}^T \mathbf{x} + \frac{1}{2} \mathbf{x}^T \frac{\partial^2 D}{\partial \mathbf{x}^2} \mathbf{x}$

 $\hat{\mathbf{x}} = -\frac{\partial^2 D}{\partial \mathbf{x}^2}^{-1} \frac{\partial D}{\partial \mathbf{x}}.$

SIFT Orientation Assignment

- Estimate keypoint orientation using local gradient vectors
	- For each keypoint, make an orientation histogram of local gradient vectors (pixels)
	- Find the dominant orientation from the main peak of the histogram
	- Create additional keypoint for second highest peak if >80%

SIFT Keypoint Descriptor

- Divide the 16x16 neighbor areas into 4x4 subareas (4x4 subwindow)
- Bin gradients within subwindow, get histogram
	- 8 bins in gradient orientation histogram
	- Rotating coordinates following orientation of keypoint -> orientation independence
	- Some clamping and normalization operations -> illumination change robustness
- Total 8 x 4 x 4 array = 128 dimensions
- Each keypoint represented by a 128D feature vector

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Application Example

• Image matching

Application Example

- Image matching
	- Compute SIFT keypoints for each image

- Image matching
	- Find best match between SIFT keypoints in 128D feature space

Image stitching

- Image stitching
	- Find SIFT keypoints and feature correspondences

- Image stitching
	- Find the right spatial transformation

Transformations

translation

affine

perspective

original

rotation

scale

Transformations

• Least-squares (LS) fitting of corresponding keypoints $(\mathbf{x}_i, \mathbf{x}_i)$

$$
E_{LS} = \sum_{i} \left\| \mathbf{r}_{i} \right\|^{2} = \sum_{i} \left\| f(\mathbf{x}_{i}; \mathbf{p}) - \mathbf{x}_{i} \right\|^{2}
$$

where \bf{p} are the parameters of the transformation in f Example for affine transformation:

 $\overline{}$ $\overline{}$ $\overline{}$ \rfloor \lceil $\begin{array}{c} \end{array}$ $\overline{}$ \parallel \lfloor $\sqrt{}$ $\overline{}$ $\overline{}$ $\overline{}$ \rfloor \lceil $\begin{array}{c} \end{array}$ $\overline{}$ \parallel \lfloor \lceil = $\overline{}$ $\overline{}$ $\overline{}$ \rfloor \exists $\begin{array}{c} \end{array}$ $\overline{}$ \parallel \lfloor $\sqrt{}$ $1 | 0 0 1 | 1$ ''*y x d e f a b c y* $\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \longrightarrow \begin{bmatrix} x & y & 0 & 0 & 1 & 0 \\ 0 & 0 & x & y & 0 & 1 \\ 0 & 0 & x & y & 0 & 1 \end{bmatrix} \begin{bmatrix} b \\ d \\ d \end{bmatrix} = \begin{bmatrix} x \\ y \end{bmatrix}$ *a x y b x* $x \quad y \quad 0 \quad 1 \parallel d$ *y e c f* $\mid a \mid$ $\begin{bmatrix} x & y & 0 & 0 & 1 & 0 \\ 0 & 0 & x & y & 0 & 1 \\ & & \dots & & & \end{bmatrix} \begin{bmatrix} b \\ d \\ e \\ c \\ \vdots \end{bmatrix} = \begin{bmatrix} x' \\ y' \\ \vdots \end{bmatrix}$ $\lfloor f \rfloor$ $\begin{array}{ccc} \cdots & & \qquad & \mathbf{e} \\ \cdots & & \mathbf{e} \end{array}$ ⇒ ⇓ $\mathbf{p} = [\mathbf{A}^T \mathbf{A}]^{-1} \mathbf{A}^T \mathbf{b}$ \leftarrow $\mathbf{A}\mathbf{p} = \mathbf{b}$ This calculation is on pixel coordinates.

• Solving for the transformation, replying on the correspondence in the overlapping area

$$
E_{LS} = \sum_{i} \left\| \mathbf{r}_{i} \right\|^{2} = \sum_{i} \left\| f(\mathbf{x}_{i}; \mathbf{p}) - \mathbf{x}_{i} \right\|^{2}
$$

- Matching results are not always perfect
	- Containing outliers
	- But most (with a rate) of the matching relationship is correct
- RANdom SAmple Consensus (RANSAC) fitting
	- Least-squares fitting is hampered by outliers
	- Some kind of outlier detection and rejection is needed
	- Better use a subset of the data and check inlier agreement
	- RANSAC does this in a iterative way to find the optimum

outlier

– Critical in 3D vision

• RANSAC

(line fitting example)

Algorithm:

- 1. **Sample** (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. **Score** by the fraction of inliers within a preset threshold of the model

• RANSAC

(line fitting example)

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• RANSAC

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Fitting and Alignment • RANSAC Algorithm: δ (line fitting example)

- 1. **Sample** (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. **Score** by the fraction of inliers within a preset threshold of the model

Stereo Matching with RANSAC

- 1. Write down the objective function
- 2. Obtain the analytical solution
	- a) Compute derivative
	- b) Compute solution
- 3. Obtain computational solution
	- a) Write in form **Ap** = **b**
	- b) Solve using pseudo-inverse (or another solver)

Stereo Matching with RANSAC

- 1. Sample a set of matching points (1 pair)
- 2. Solve for transformation parameters
- 3. Score parameters with number of inliers
- 4. Repeat steps 1-3 N times

Feature for Classification

• SIFT-based texture classification – how to do this?

Problem: the number of SIFT keypoints (and thus the number of SIFT feature descriptors) may vary highly between images

- Global encoding of local SIFT features
	- Integrate the local features (SIFT keypoint descriptors) of an image into a global vector to represent the whole image

- Most popular method: Bag-of-Words (BoW)
	- The variable number of local image features are encoded into a fixed-dimensional histogram to represent each image

- Bag-of-Words (BoW) step 1
	- Create the vocabulary from the set of local descriptors (SIFT keypoint descriptors) extracted from the training data
	- This vocabulary represents the categories of local descriptors

- Bag-of-Words (BoW) step 1
	- Extracting local feature descriptors
	- Clustering
		- k-means clustering is one of the simplest and most popular unsupervised learning approaches that perform automatic clustering (partitioning) of the training data into multiple categories

- Bag-of-Words (BoW) step 1
	- K-means clustering:
		- o Initialize: *k* cluster centres, typically randomly
		- o Iterate: 1) Assign data (feature vectors) to the closest cluster (Euclidean distance) 2) Update cluster centres as the mean of the data samples in each cluster
		- o Terminate: When converged or the number of iterations reaches the maximum

- Bag-of-Words (BoW) step 2
	- The cluster centres are the "visual words" which form the "vocabulary" that is used to represent an image
	- An individual local feature descriptor (e.g. SIFT keypoint descriptor) is assigned to one visual word with the smallest distance

- Bag-of-Words (BoW) step 2
	- For an image, the number of local feature descriptors assigned to each visual word is computed
	- The numbers are concatenated into a vector which forms the BoW representation of the image

• Example feature vectors of texture images

Image from Cordelia Schmit

• SIFT-based texture classification

- 1. SIFT feature extraction 2. BoW encoding 3. Classification
-

• SIFT-based classification

- Local features can be other types of features, not just SIFT – LBP, SURF, BRIEF, ORB
- There are also more advanced techniques than BoW
	- VLAD, Fisher Vector
- A very good source of additional information is VLFeat.org
	- <http://www.vlfeat.org/>

• HOG describes the distributions of gradient orientations in localized areas and does not require initial segmentation

N. Dalal and B. Triggs, "Histograms of oriented gradients for human detection," Computer Vision and Pattern Recognition 2005.<https://doi.org/10.1109/CVPR.2005.177>

- HoG feature for image description
	- Compute gradients
	- Bin gradients
	- Aggregate blocks (4x4, 16x16 cells)
	- Normalize gradient magnitudes
- Not reliant on magnitude, just direction
	- Invariant to some lighting changes
- Dense on images
- Object detection

- Step 1: Calculate gradient magnitude and orientation at each pixel with a gradient operator \Rightarrow gradient vector
- Step 2: Divide orientations into *N* bins and assign the gradient magnitude of each pixel to the bin corresponding to its orientation => cell histogram
	- For example 9 bins evenly divided from 0 to 180 degrees

https://medium.com/@dnemutlu/hog-feature-descriptor-263313c3b40d

• Step 3: Concatenate and block-normalise cell histograms to generate detection-window level HOG descriptor

• Detection via sliding window on the image

• Detection via sliding window on the image

HOG feature map **Detector** response map

A response map could be computed for example as follows:

- o Compute the HOG descriptor for many example windows from a training dataset
- o Manually label each example window as "person" or "background"
- o Train a classifier (such as a SVM) from these example windows and labels
- o For each new (test) image, predict the label of each window using this classifier

• Human detection

<https://www.pyimagesearch.com/2015/11/09/pedestrian-detection-opencv/>

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Shape Features

- **Shape** is an essential feature of material objects that can be used to identify and classify them
- Example: object recognition

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Basic Shape Features

• Simple geometrical shape descriptors

Compactness:

Ratio of the area of an object to the area of a circle with the same perimeter

Circularity:

Ratio of 4π times the area of an object to the second power of its perimeter $(4\pi A/P^2)$ equals 1 for a circle)

Basic Shape Features

• Simple geometrical shape descriptors

Elongation:

Ratio between the length and width of the object's bounding box

Eccentricity:

Ratio of the length of the minor axis to the length of the major axis

Boundary Descriptors

- Chain code descriptor
	- The shape of a region can be represented by labelling the relative position of consecutive points on its boundary
	- A chain code consists of a list of directions from a starting point and provides a compact boundary representation

Shape Context

- **Shape context** is a point-wise local feature descriptor
	- Pick *n* points on the contour of a shape
	- $-$ For each point p_i construct a histogram h_i of the relative coordinates of the other $n-1$ points => this is the shape context of p_i

$$
h_i(k) = #\{q \neq p_i : (q - p_i) \in \text{bin}(k)\}\
$$

S. Belongie, J. Malik, J. Puzicha (2002), "Shape matching and object recognition using shape contexts," IEEE Transactions on Pattern Analysis and Machine Intelligence 24(4):509-522.<https://doi.org/10.1109/34.993558>

Learning Representations

- Handcrafted features
	- LBP, SIFT, HoG, BoW ….
	- Used for very long time
	- Worked well for many applications
- Can the feature engineering process be automatic?
	- Finding discriminative signatures automatically and systematically
- Learning for reorientations
	- a brief overview

Learning Representations

• Supervised learning for representations

– With some specific task

- Unsupervised learning for representations
	- Learning with some protext tasks
		- Image reconstruction

Unsupervised Representation Learning

- Representation learning still needs a loss function to provide supervision signal
	- Reconstructing the input image
		- L2 $/$ L1 $/$ GAN loss
		- Learning representations that can reconstruct the image
- Different models/methods
	- Sparse coding
	- (Deep) autoencoders
	- Generative Adversarial Network based feature learning

Sparse Coding

- Learning to obtain a dictionary for representing each image/patch with a sparse vector
- The sparse vector can be used as descriptors for downstream tasks, such as classification

Autoencoder

- (Deep) neural network trained with the task for reconstructing images
	- encoder, decoder
	- Extracted features (from encoder) can be used for downstream tasks
	- Can be very large-scale & powerful

Supervised Representation Learning

- Deep neural networks
	- End-to-end model
		- Image features output of the task
	- will be discussed more in week 7

Summary

- What and why of feature representation
	- Feature representation is essential in solving almost all types of computer vision problems
- How of feature representation
	- Different feature extractors/descriptors
		- Classical approaches
			- Color features
			- Haralick texture features, LBP, SIFT, BoW, HoG, Shape descriptors
		- Representation learning
			- Unsupervised/supervised representation learning
	- Application cases in various computer vision applications
		- Classification
		- RANSAC for stereo matching (robust fitting)
		- Detection
		- …

References and Acknowledgements

- Szeliski, Chapter 4 (in particular Sections 4.1.1 to 4.1.3 and 4.3.2), Chapter 6 (in particular Sections 6.1.1 to 6.1.4)
- Some content are extracted from the above resource, James Hays slides, slides from Michael A. Wirth, slides from Cordelia Schmit
- L. Liu et al., From BoW [to CNN: two decades of texture representation for](https://doi.org/10.1007/s11263-018-1125-z) [texture classification](https://doi.org/10.1007/s11263-018-1125-z)*,* International Journal of Computer Vision, 2019
- And other resources as indicated by the hyperlinks